



Application of Active Disturbance Rejection Control in Superconducting Radio Frequency Cavities

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U.S. DEPARTMENT OF
ENERGY

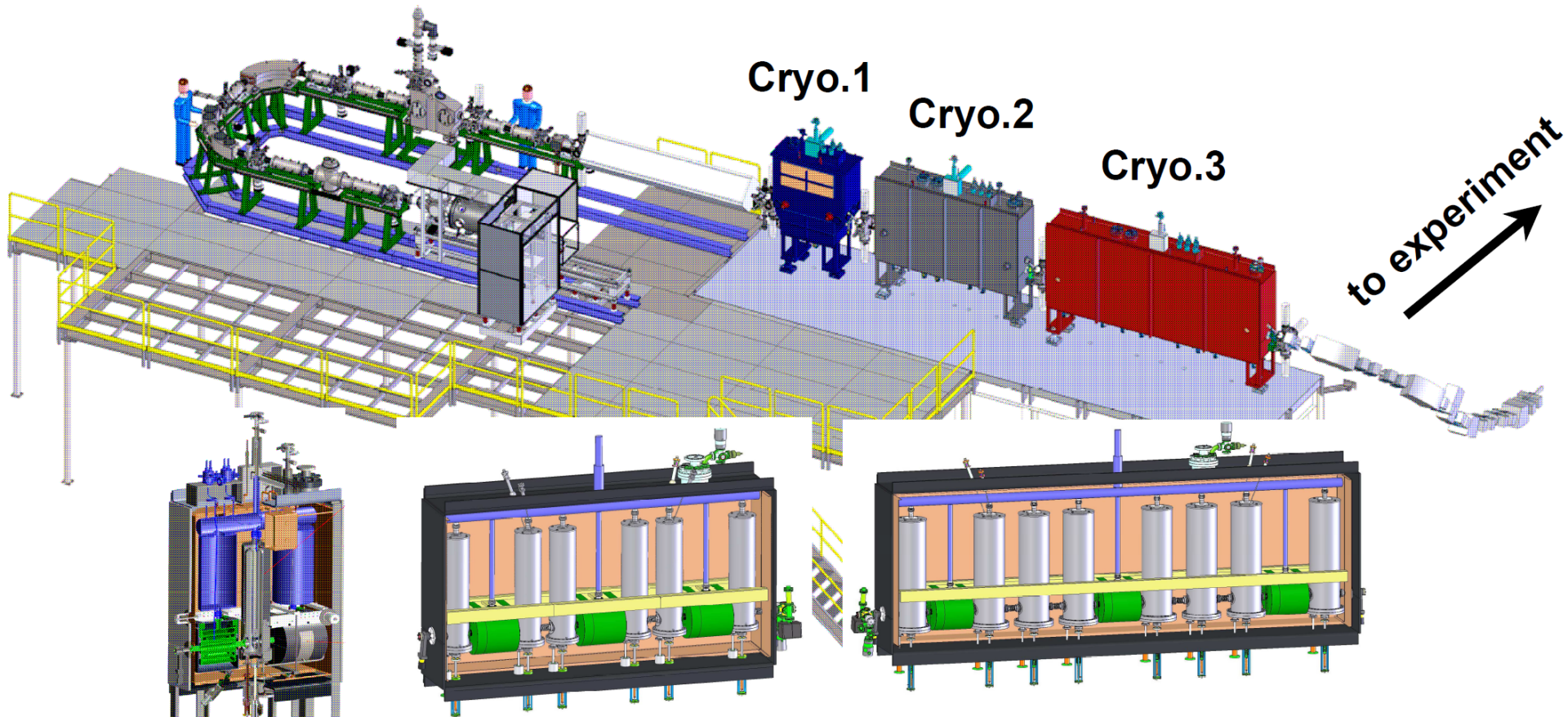
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Outline

- Previous Results on Microphonics Mitigation
- More on Active Disturbance Rejection Control (ADRC)
- ADRC Applications at FRIB/NSCL
 - Beam Loading
 - FPGA Implementation
 - Tuner Control
 - ReA3 Vibration Test

First Application of ADRC in SFR Caverns

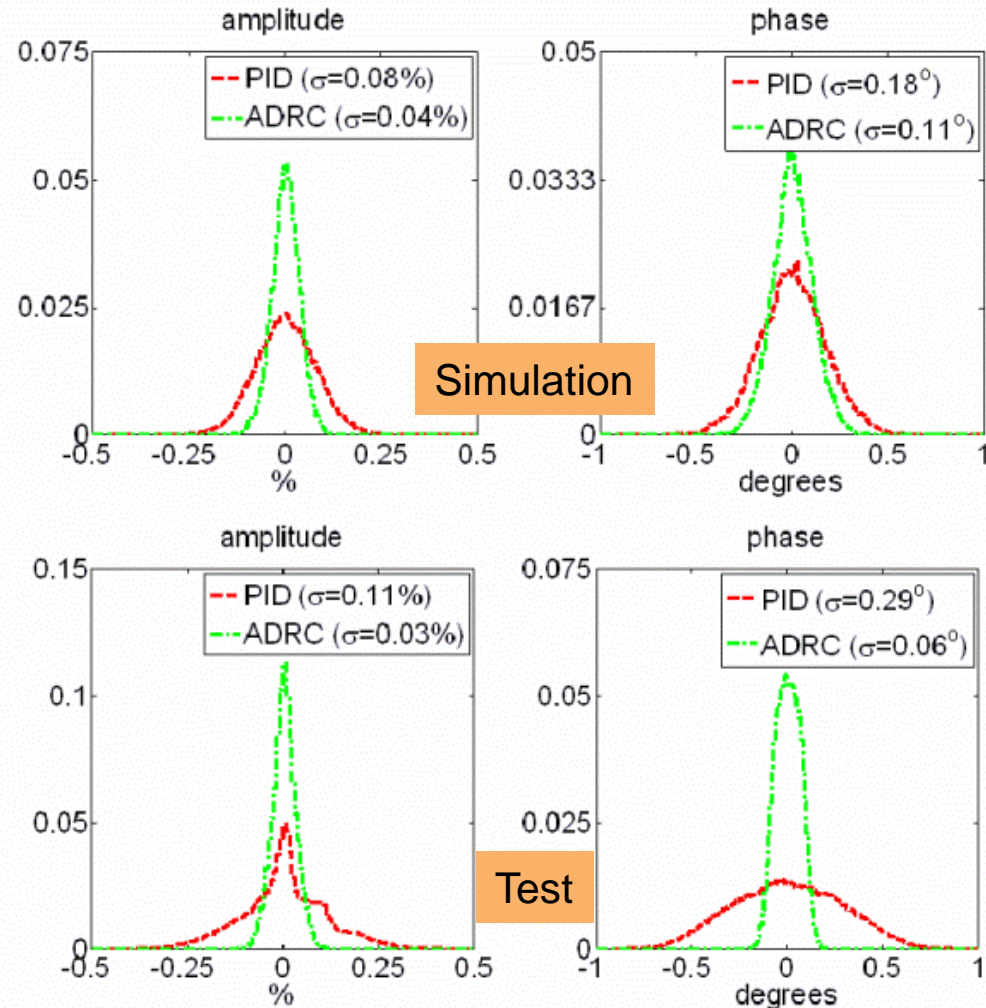
- Application of ADRC at NSCL
 - Spring 2010
 - Narrow bandwidth and sensitive to vibrations
 - ReA3 is on the balcony and the vibration is severe



Previous Results

- Demonstrated the effectiveness of ADRC [Vincent, 2011]

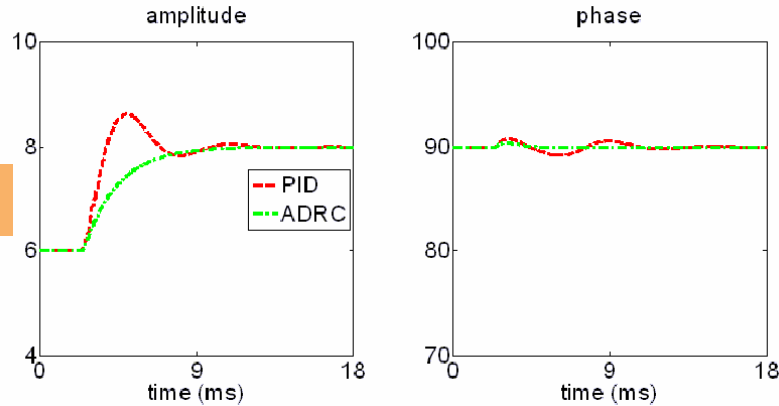
- Two times improvement in simulation (top)
- Four times improvement in tests (bottom)
- Running on ReA3 since Jan. 2011



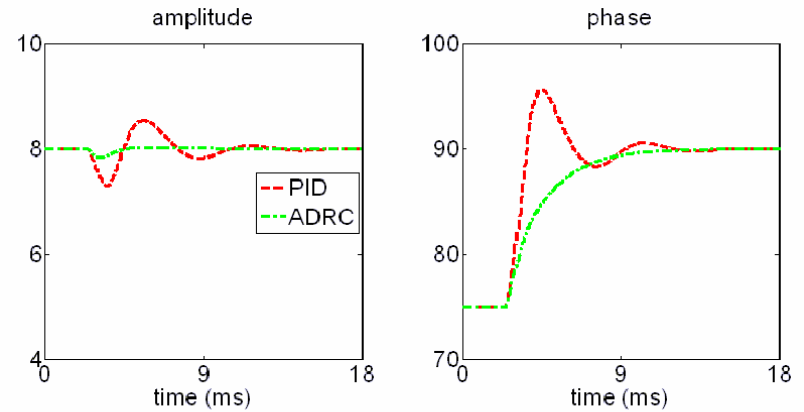
Better Decoupling

Simulation

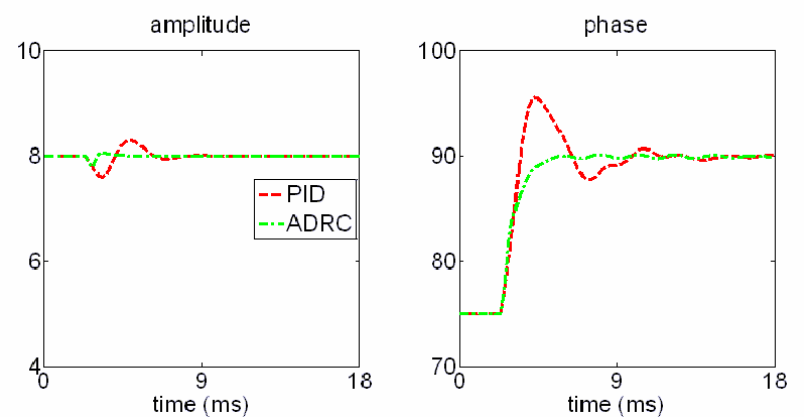
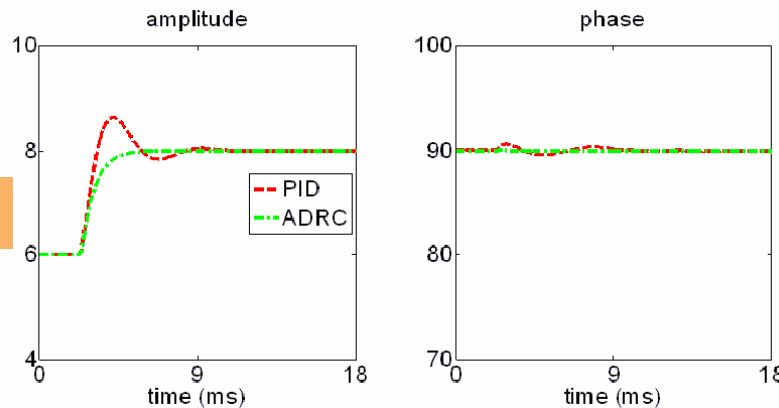
Amplitude Set-point Change



Phase Set-point Change



Test



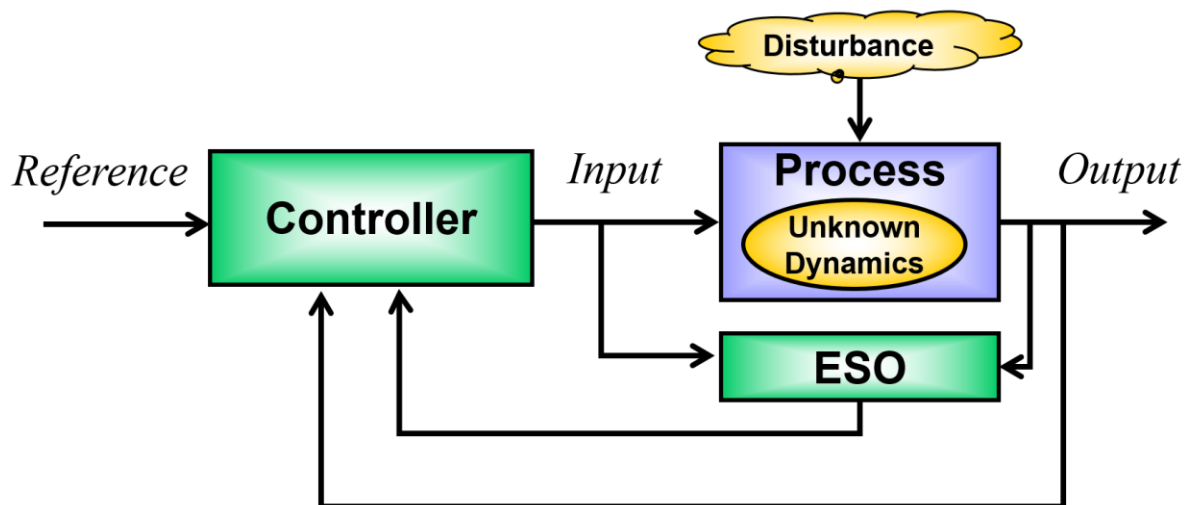
Active Disturbance Rejection Control

- Proposed by Prof. Han in 1998 [Han 2009]
 - Treat external disturbance and system uncertainty as the *total disturbance*
 - Estimation the total disturbance using an extended state observer (ESO)
 - Cancel it in the controller

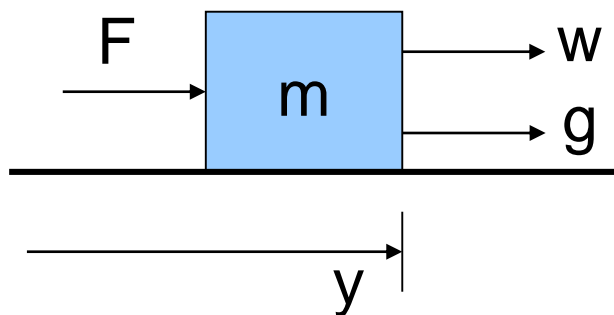
- Other Similar Methods

- Unknown Input Observer
- Disturbance Observer
- Perturbation Observer

(only deal with external disturbance)



ADRC Formulation - A Simple Example



$$m\ddot{y} = F + \boxed{g(y, \dot{y}, t)} + \boxed{w(t)}$$

Internal External
Uncertainty Disturbance

$$b = 1/m \quad u = F$$

$$f(y, \dot{y}, w, t) = (g(y, \dot{y}, t) + w(t))/b$$

$$\ddot{y} = bu + \boxed{f(y, \dot{y}, w, t)}$$

Total Disturbance

$$u = (-\hat{f} + u_0)/b$$

$$\ddot{y} = u_0 + (f - \hat{f}) \approx u_0$$

Disturbance Cancellation

$$u_0 = k_p e + k_d \dot{e}$$

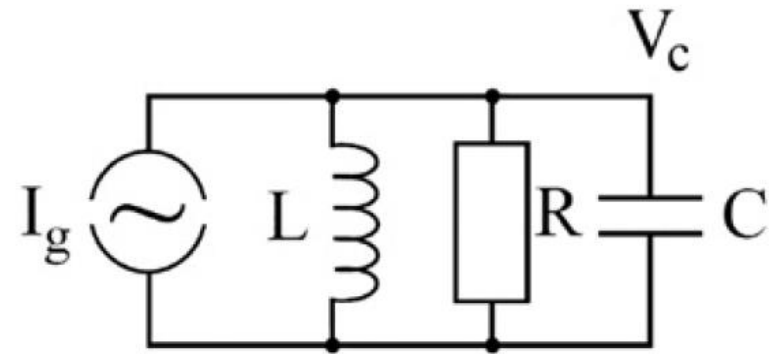
Simple Controller

SRF Cavity Model

■ Parallel RLC Circuit Model

$$\frac{d^2 \vec{V}_c}{dt^2} + \frac{\omega_0}{Q} \frac{d\vec{V}_c}{dt} + \omega_0^2 \vec{V}_c = \frac{R\omega_0}{Q} \frac{d\vec{I}_g}{dt}$$

$$\omega_0 = 1/\sqrt{LC} \quad Q = R\sqrt{C/L}$$



■ Approximation

$$\begin{aligned} \dot{V}_{cI} + \omega_{1/2} V_{cI} + \Delta\omega V_{cQ} &= \omega_{1/2} V_{gI} \\ \dot{V}_{cQ} + \omega_{1/2} V_{cQ} - \Delta\omega V_{cI} &= \omega_{1/2} V_{gQ} \end{aligned} \quad \begin{cases} I = A \cos P \\ Q = A \sin P \end{cases}$$

ADRC Design for SRF Cavity

$$\dot{V}_{cI} + \omega_{1/2} V_{cI} + \Delta\omega V_{cQ} = \omega_{1/2} V_{gI}$$

$$\dot{V}_{cQ} + \omega_{1/2} V_{cQ} - \Delta\omega V_{cI} = \omega_{1/2} V_{gQ}$$

■ Algorithm

- System

$$\dot{y} = f(y, w, t) + bu$$

- Observer

$$\dot{\hat{x}}_1 = \hat{x}_2 + \hat{b}u + l_1(y - \hat{x}_1) \quad \text{Estimation of } y$$

$$\dot{\hat{x}}_2 = l_2(y - \hat{x}_1) \quad \text{Estimation of } f$$

- Controller

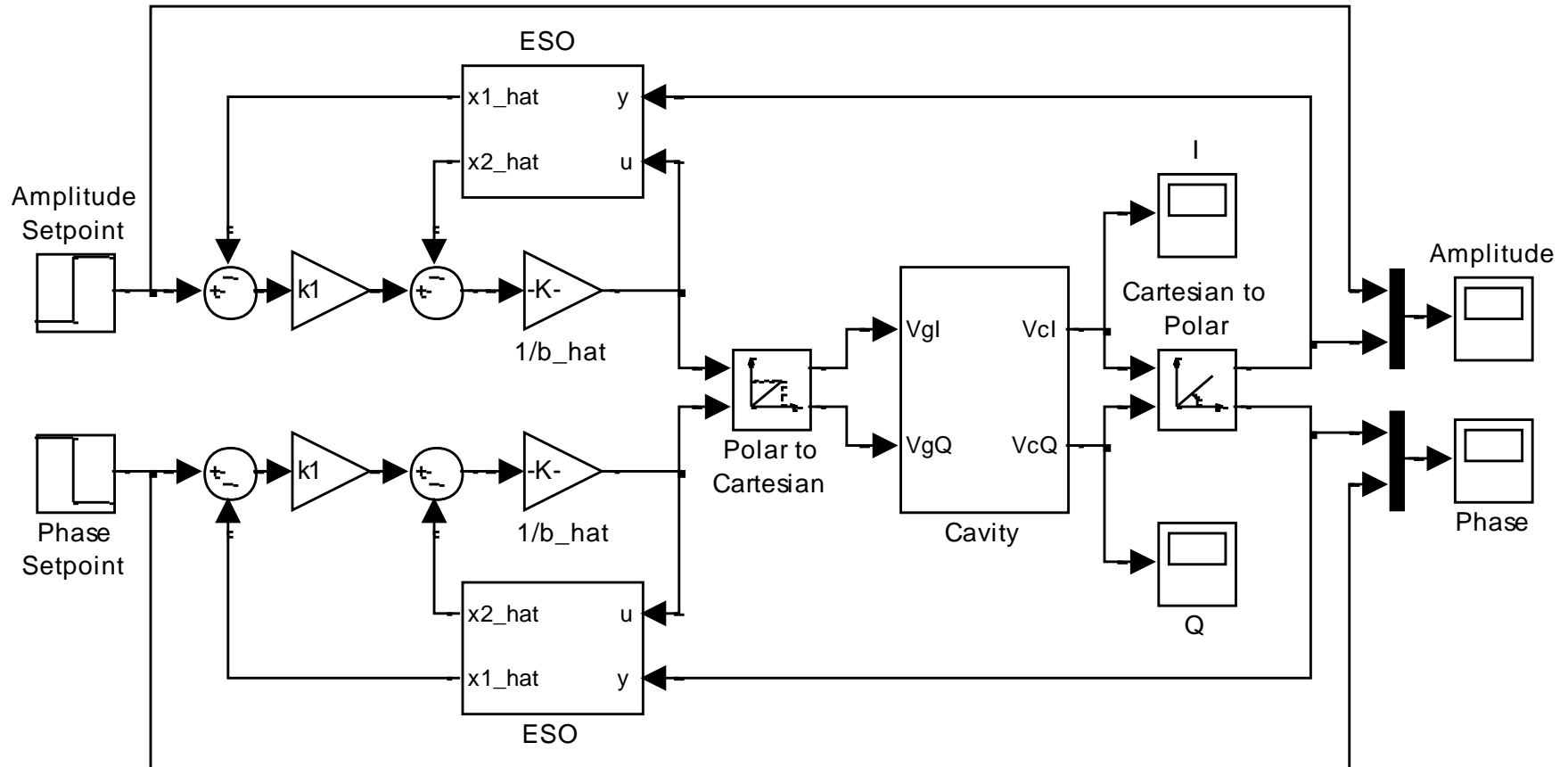
$$u = (k_1(r - y) - \hat{x}_2) / \hat{b}$$

Disturbances in SRF Cavities

- Microphonics
 - Ground vibration;
 - Pumps: Helium pump, vacuum pump, etc.
- Lorentz Force
- Beam Dynamics
 - Beam loading;
 - Beam current variation.
- Others
 - Hysteresis in piezo tuner;
 - Non-linearity in solid state amplifier.

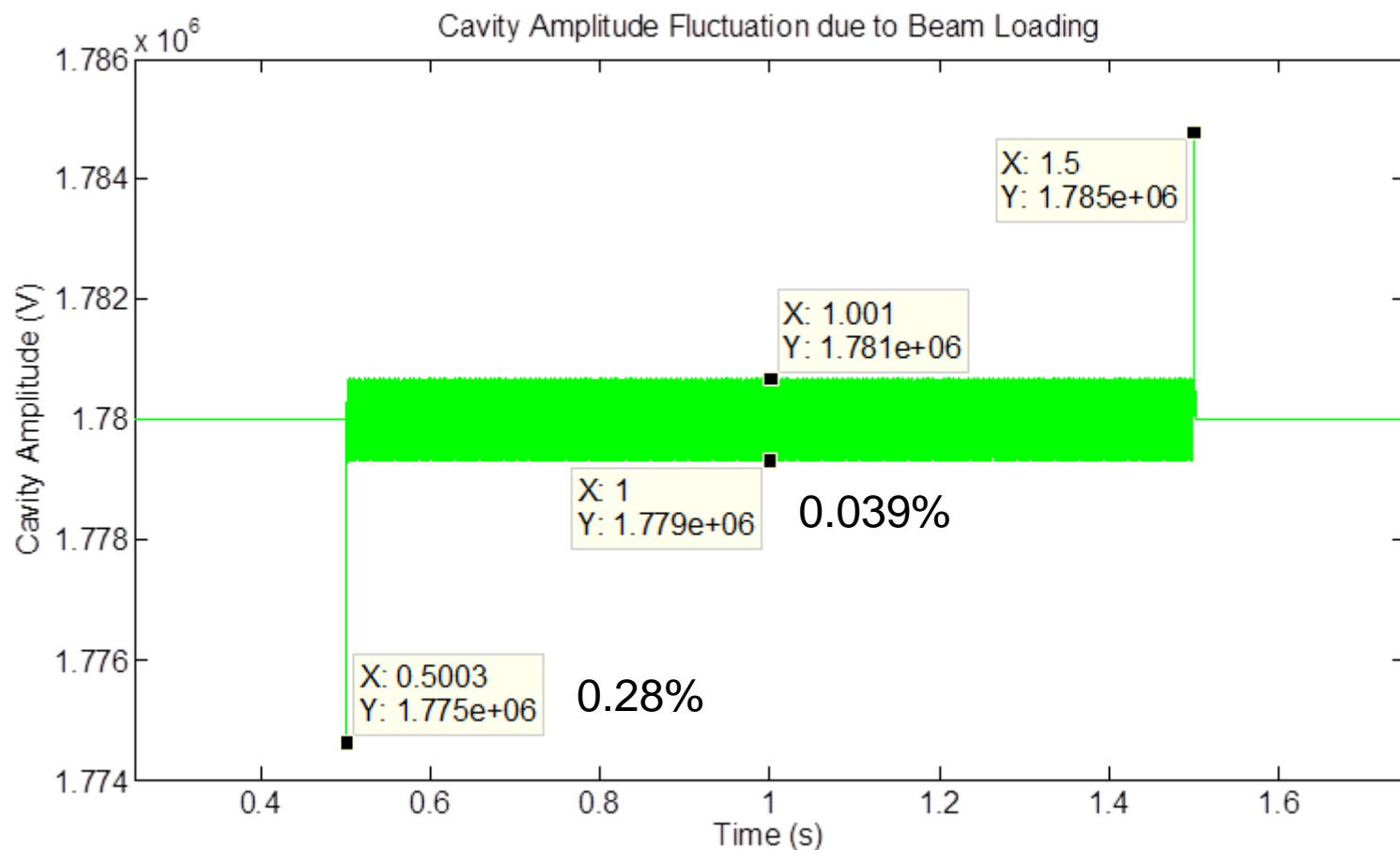
Beam Loading [Zheng 2012]

■ Simulation Model



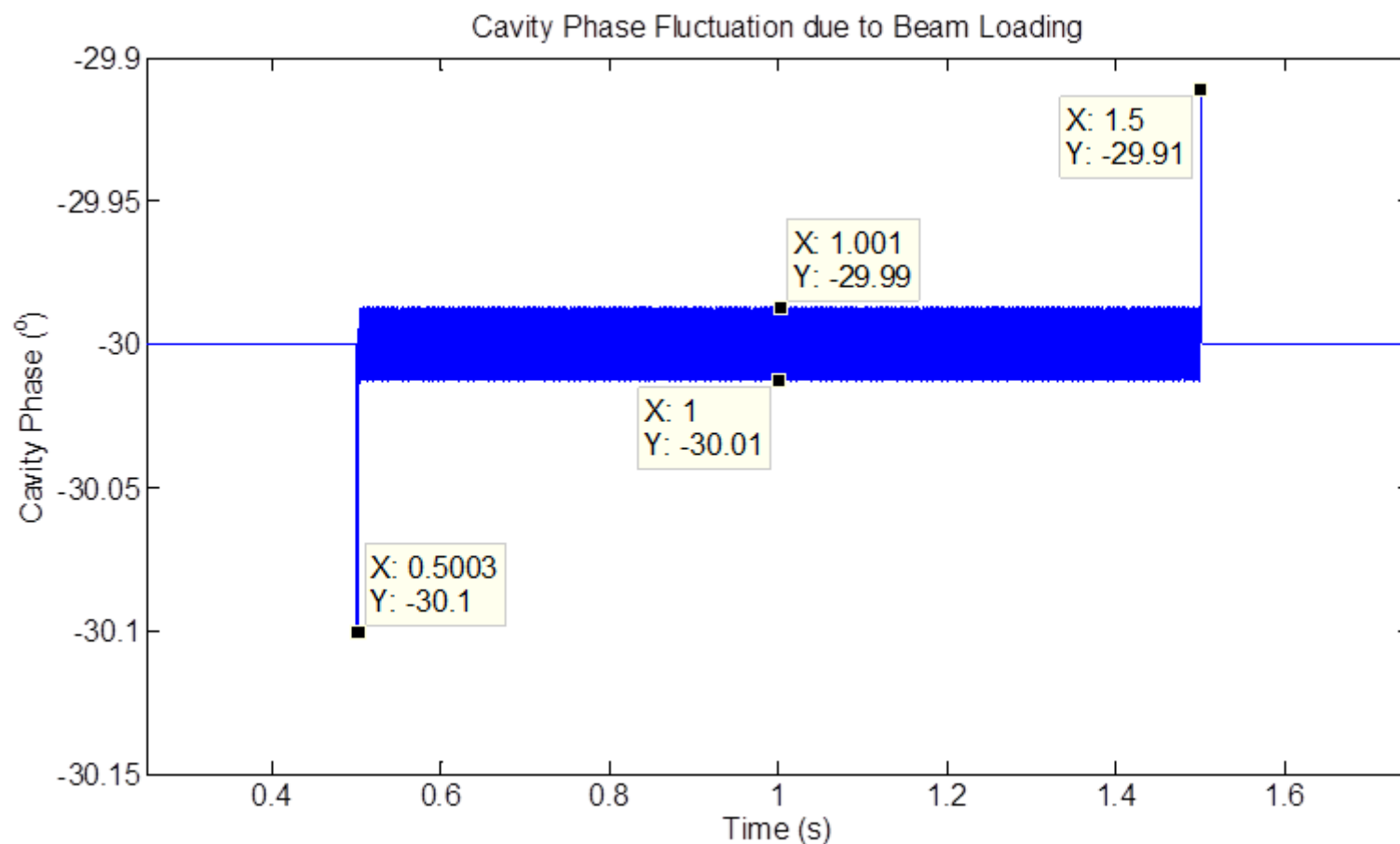
Results under Beam Loading

■ Amplitude Response



Results under Beam Loading

Phase Response



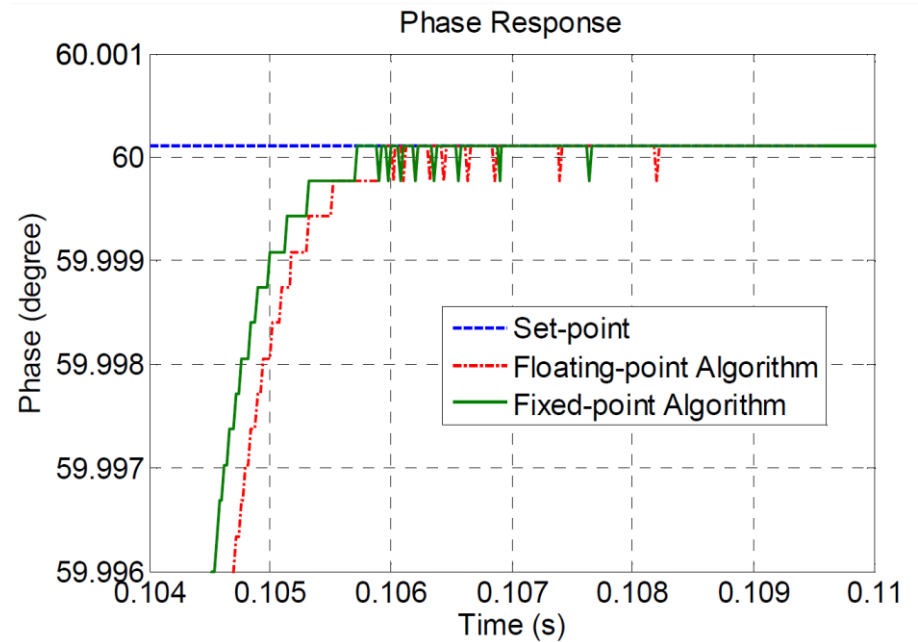
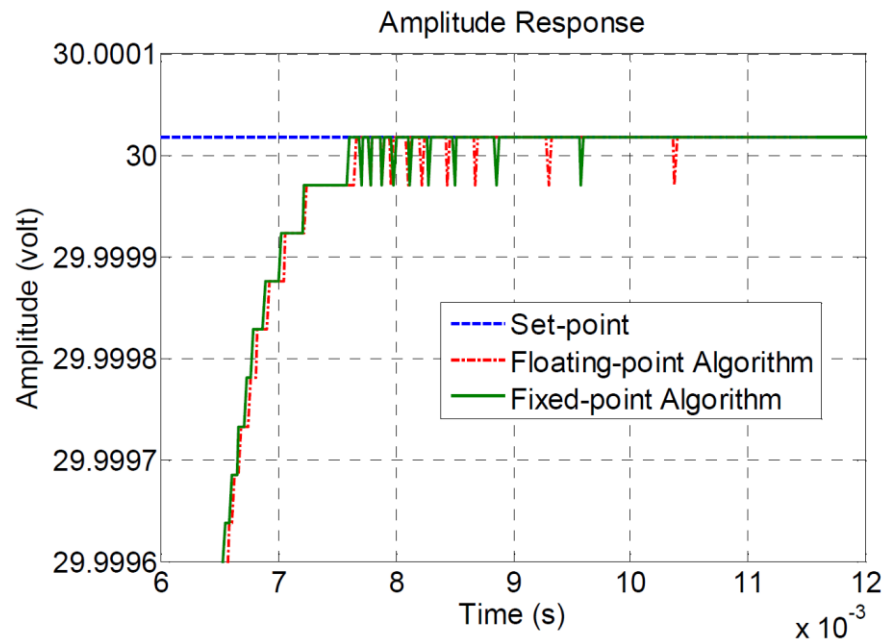
FPGA Implementation [Zhao 2013]

- To increase the sampling rate
 - Potential performance improvement
 - » Observer bandwidth can be further increased;
 - Expands the working range of the SEL
 - » 1/12 of the sampling rate [Zhao 2011];
 - » Currently around 4 KHz (50 KHz in DSP);
- No processor planned in LLRF controller (long term)
 - ADRC algorithm has to go into the firmware;



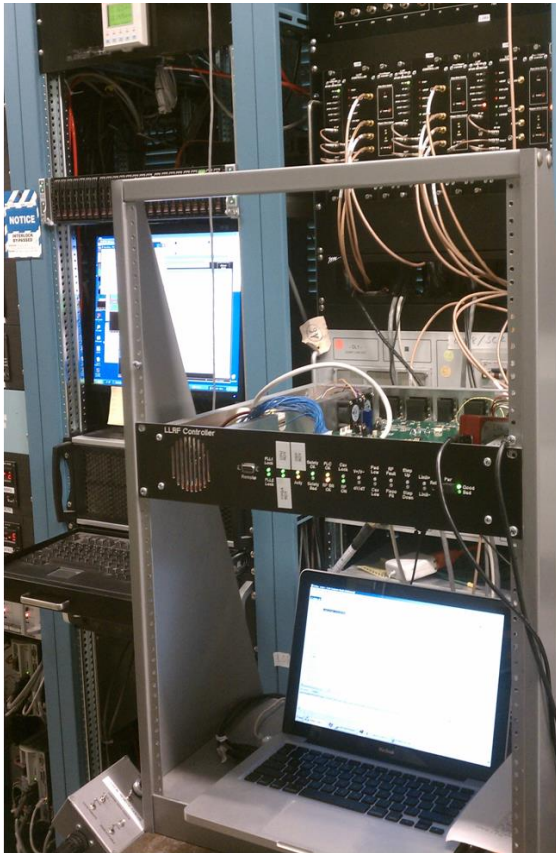
Simulation Results

■ A Comparison between Fixed-point and Floating-point Algorithms



Hardware Test Verification

- LLRF Controller PED 1
- ReA3 L088, Dec. 2012

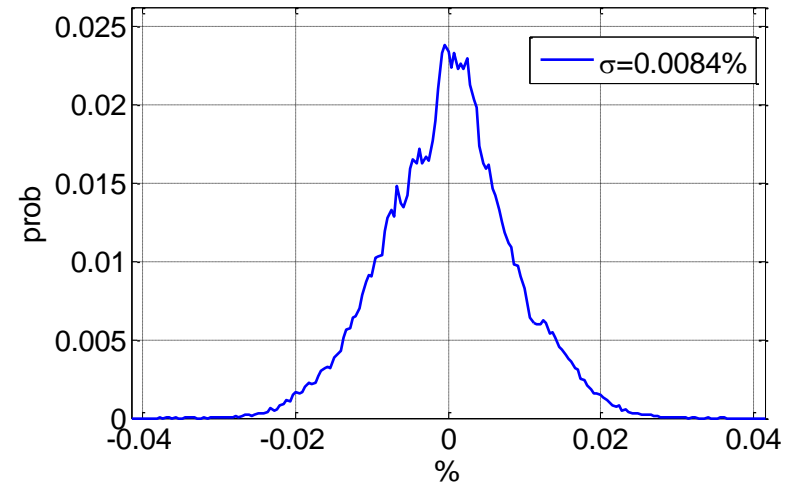


FRIB Specs:

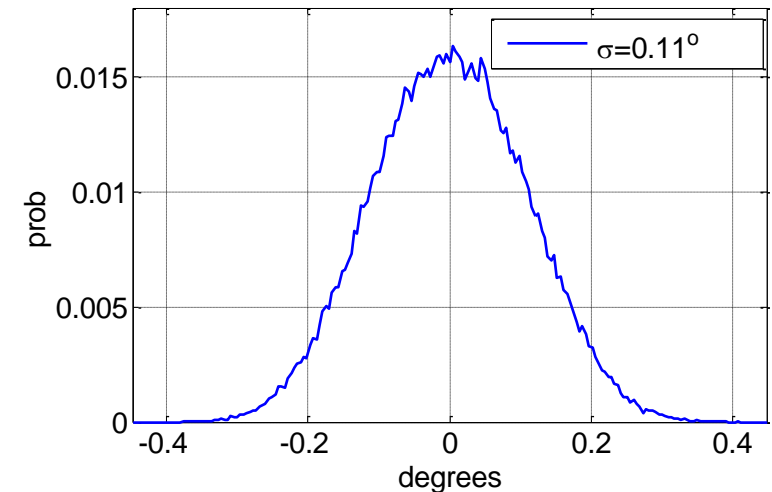
Amplitude (RMS) :
<0.25%

Phase (RMS):
<0.25 degrees

PDF of Cavity Amplitude Deviation



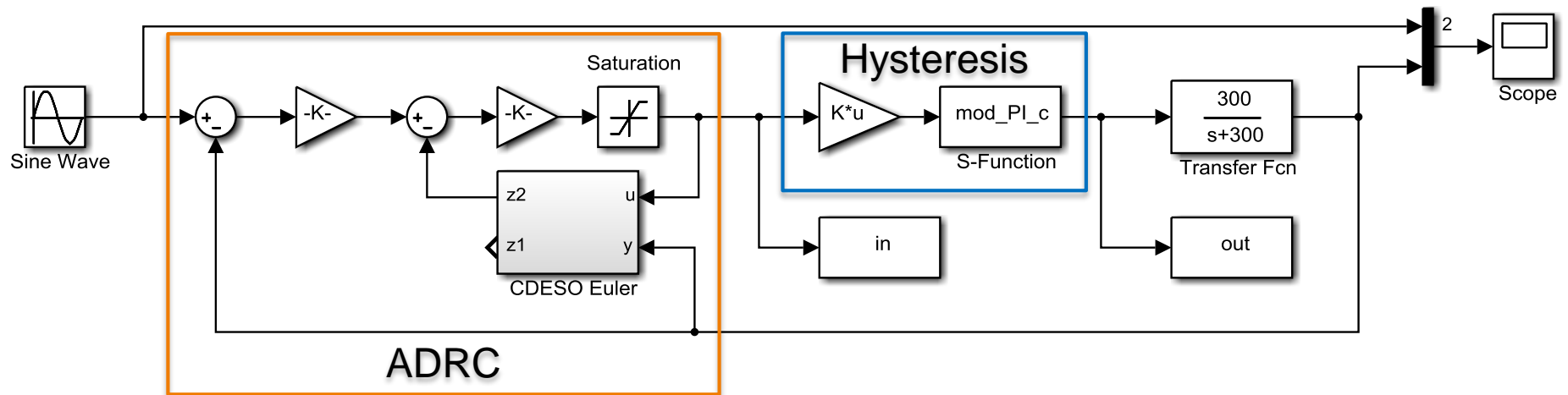
PDF of Cavity Phase Deviation



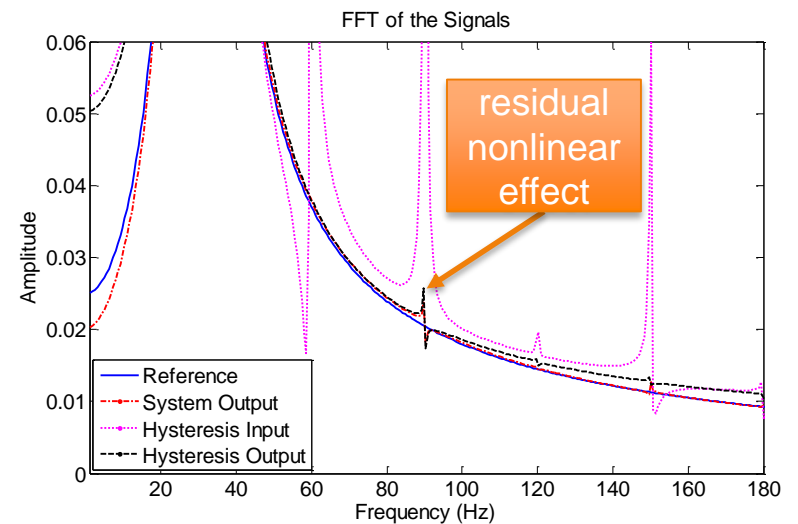
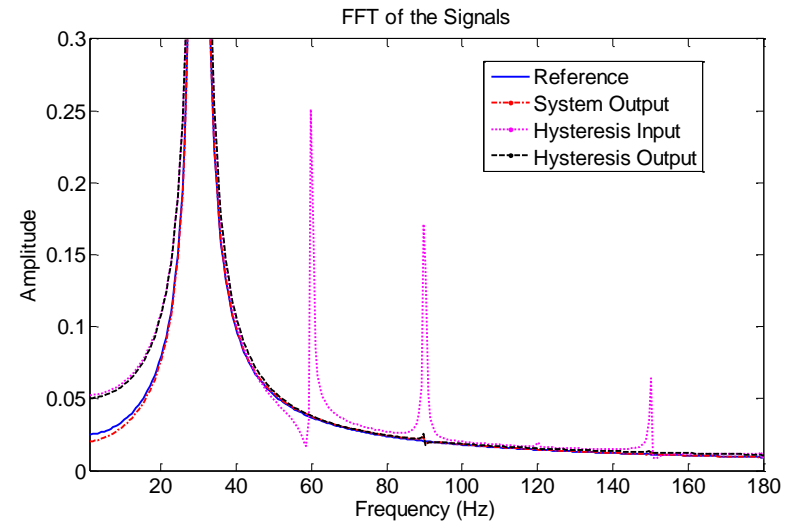
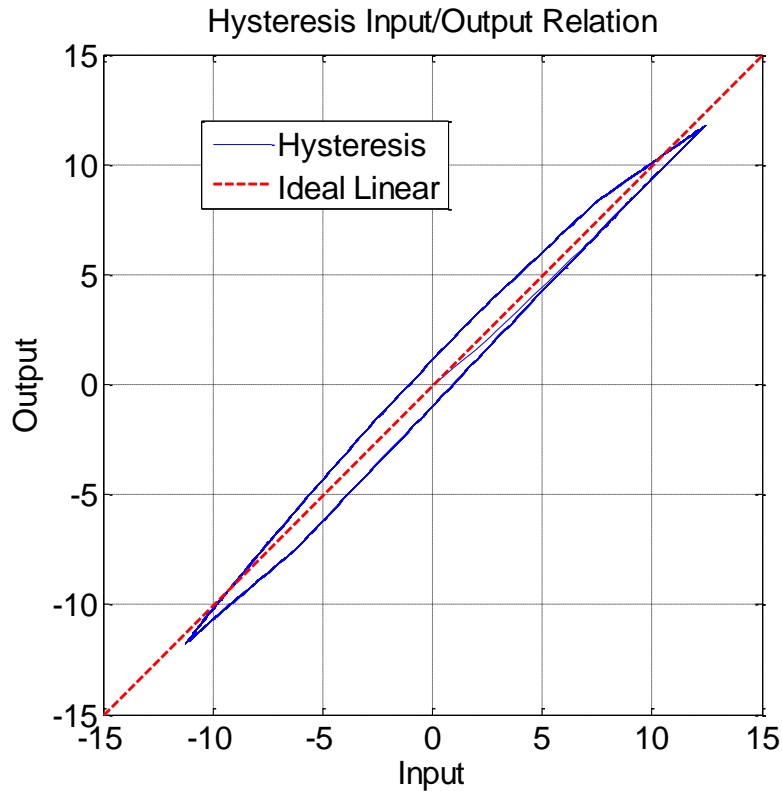
Tuner Control

■ Fast Piezoelectric Tuner

- Hysteresis compensation [Goforth 2012]

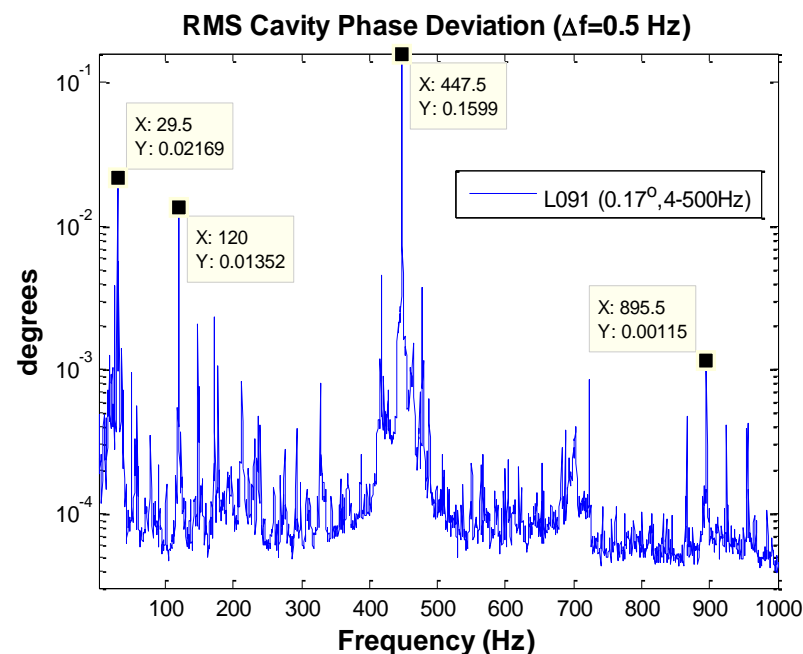
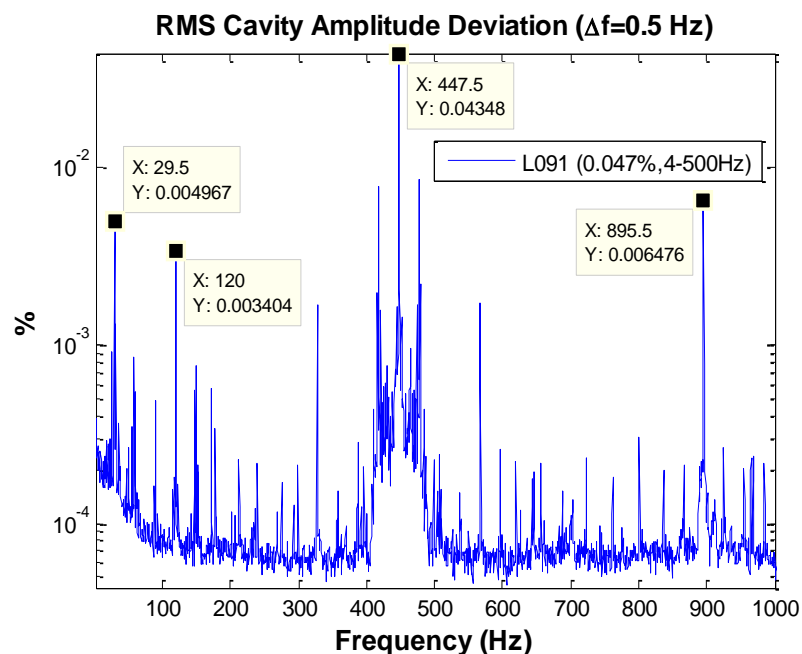


Simulation Results

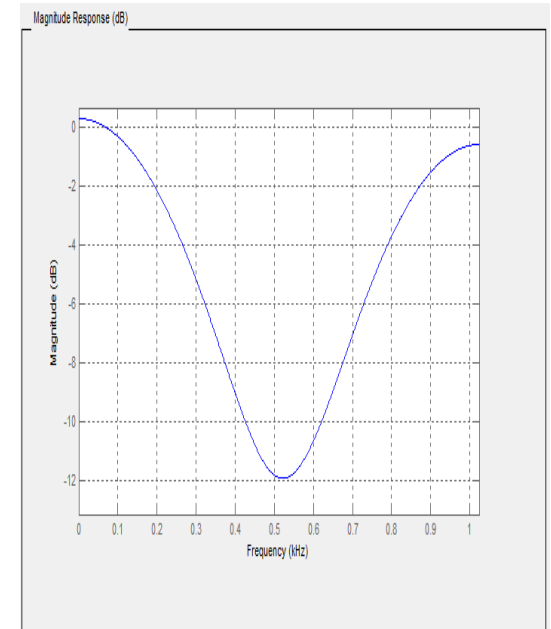
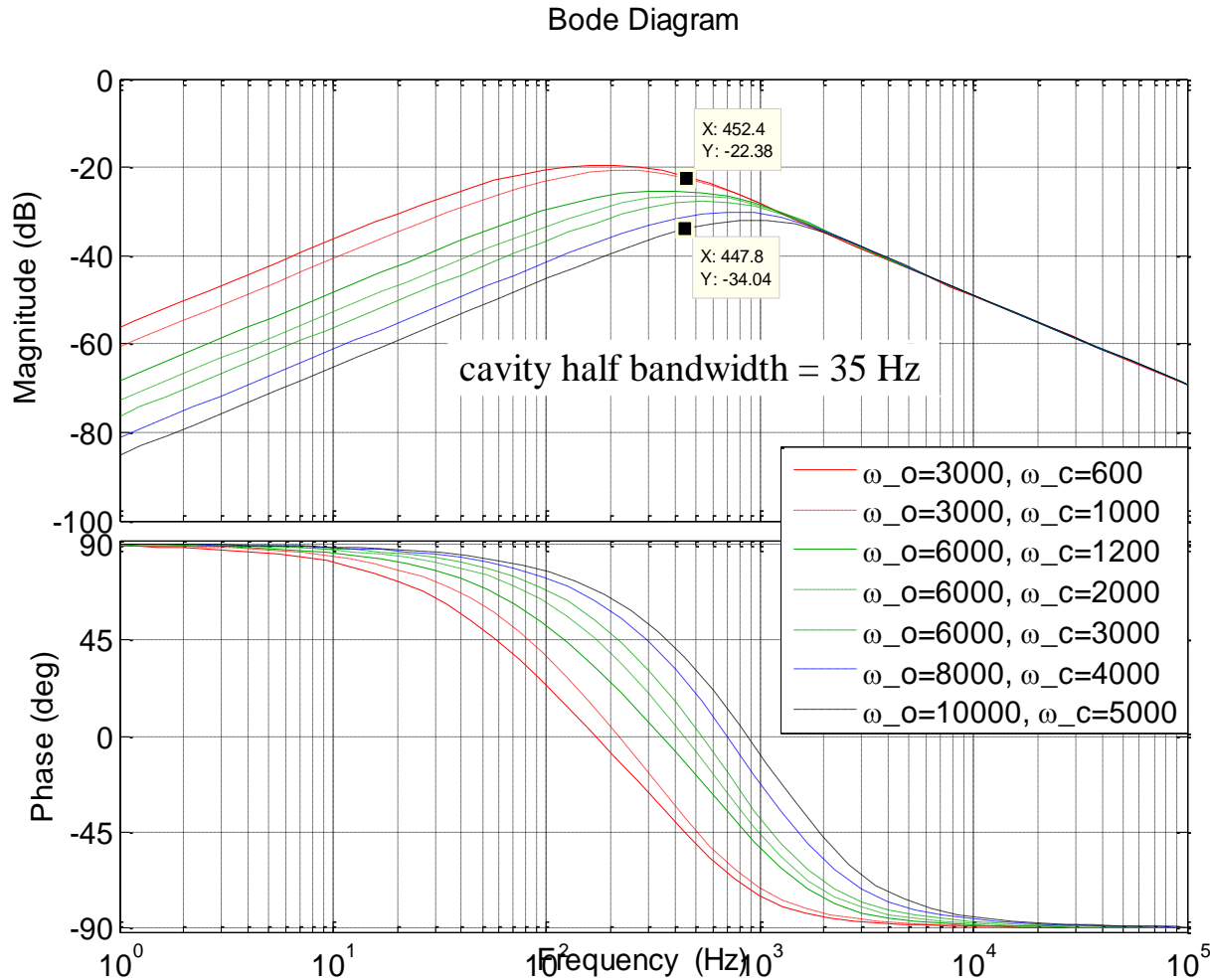


ReA3 Vibration Test

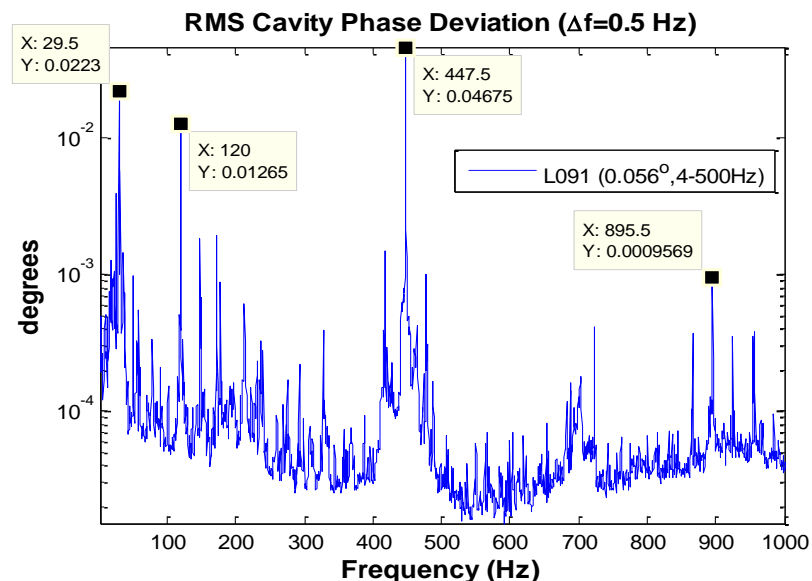
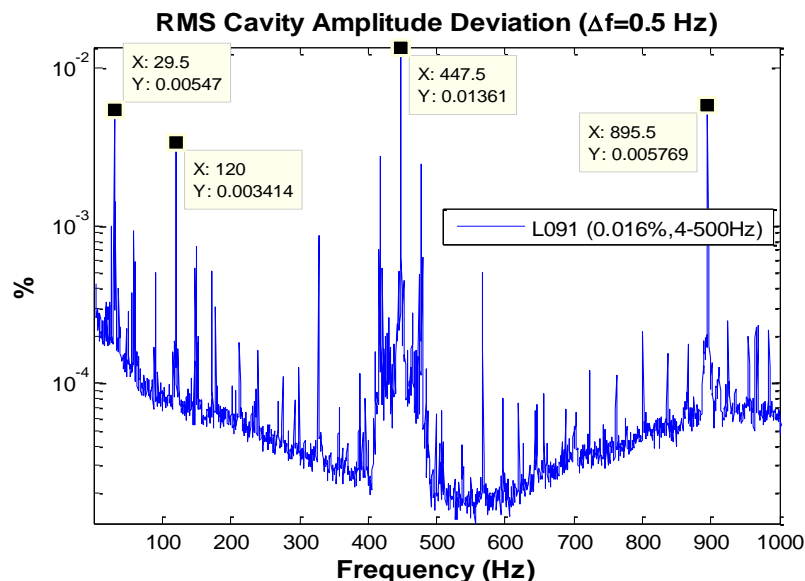
■ Original Measurement



Disturbance Rejection Characteristics of the ADRC Controller



Filtered Data



Pumps		Controller				Cavities								Acceleration			
a1	a2	Amp		Phase		L077		L082		L089		L091		EW	NS	EW	UD
		ω_o	ω_c	ω_o	ω_c	Amp	Phase	Amp	Phase	Amp	Phase	Amp	Phase	leg	leg	side	top
ON	ON	3000	600	3000	600	0.057	0.076	0.023	0.079	0.011	0.024	0.041	0.17	13	101	756	102
ON	ON	10000	5000	10000	5000	0.021	0.013	0.0045	0.017	0.0032	0.0061	0.013	0.062	13	106	692	116
OFF	OFF	3000	600	3000	600	0.074	0.09	0.0054	0.023	0.0039	0.008	0.0027	0.01	3.8	21.4	5.2	10.2

References

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- [4] S. Zhao, “LLRF control for superconducting RF cavities,” internal research report, National Superconducting Cyclotron Laboratory, 2011, unpublished.
- [5] S. Zhao *et al.*, “Fixed-point implementation of active disturbance rejection control for superconducting radio frequency cavities,” *American Control Conference*, pp. 2699-2704, 2013.
- [6] Z. Zheng *et al.*, “ADRC control for beam loading and microphonics,” *LINAC 2012*, pp. 615-617, 2012.
- [7] Z. Zheng *et al.*, “Piezo-electric tuner study for SRF cavity,” *PAC 2013*, to be presented, 2013.

Questions



Thanks for your attention!

감사합니다 Natick
Grazie Danke Ευχαριστίες Dalu
Thank You Köszönöm
Спасибо Dank Tack
谢谢 Merci Gracias
ありがとう Seé
obligado

